

1. Of 130 students in Math 3081, 88 study every day, 73 work on WeBWorK every day, and 54 do both.
 - (a) How many students study every day but don't work on their homework every day?
 - (b) How many students neither study nor work on their homework every day?

2. Find the number of 5-letter strings that can be made from the letters ABCDEFG such that:
 - (a) The string starts with AG.
 - (b) The string has no repeated letters.
 - (c) The string contains neither C nor G.
 - (d) The string has at least one repeated letter.
 - (e) The string contains at least one B.
 - (f) The string has no doubled letters (no AA, ...).

3. A tennis team of 14 people selects 3 nonoverlapping pairs of players to make doubles teams. Find the number of ways of making these selections if the order of the 3 pairs (a) matters, (b) does not matter.

4. A fair coin is flipped 10 times. Find the probabilities of the following events:
 - (a) All the flips are heads.
 - (b) The first and last flips are heads.
 - (c) Exactly 4 flips are tails.
 - (d) At least 8 heads are obtained.
 - (e) The first three flips are all the same.
 - (f) There are more tails than heads.

5. Three standard 6-sided dice of different colors are rolled. Find the probabilities of the following events:
 - (a) Three of a kind (all dice equal).
 - (b) Pair (two dice equal, third different).
 - (c) No pair (all dice different).
 - (d) 6-3-2 in some order.
 - (e) No 6s or 5s are rolled.
 - (f) At least one 6 is rolled.
 - (g) 3-3-3, given no 6s or 5s are rolled.
 - (h) 1-1-5 in some order, given a pair is rolled.
 - (i) 6-3-2 in some order, given a 6 is rolled.
 - (j) 6-3-2 in some order, given no pair is rolled.

6. An urn contains 10 red and 8 orange balls. 4 balls are drawn without replacement. Find the probabilities that:
 - (a) All 4 balls are red.
 - (b) 1 ball is red and 3 are orange.
 - (c) All 4 balls are red, given that ≥ 1 is red.
 - (d) Ball #1 is orange, given that ≥ 3 are red.

7. Suppose A and B are events such that $P(A) = 0.4$, $P(B|A) = 0.8$, and $P(B|A^c) = 0.1$. Find:
 - (a) $P(A^c)$.
 - (b) $P(A \cap B)$.
 - (c) $P(A^c \cap B)$.
 - (d) $P(B)$.
 - (e) $P(B^c)$.
 - (f) $P(A \cup B)$.
 - (g) $P(A \cap B^c)$.
 - (h) $P(A|B)$.
 - (i) $P(B^c|A)$.
 - (j) $P(A^c \cap B^c)$.
 - (k) $P(A^c|B^c)$.
 - (l) $P(A \cup B^c)$.

8. Suppose $P(A) = 0.3$ and $P(B) = 0.4$. Find $P(A \cup B)$ if A and B are (a) mutually exclusive, (b) independent.

9. Market research shows that 15% of Americans and 90% of Canadians like poutine. A math conference has 40% Canadian attendees and 60% American attendees. Find the probabilities that:
 - (a) A random attendee is American and likes poutine.
 - (b) A random attendee likes poutine.
 - (c) A random attendee who likes poutine is American.
 - (d) A random poutine-disliking attendee is Canadian.

10. Given that discrete random variables X and Y have probability distributions as below, find:

n	0	1	2	3	4
$P(X = n)$	0.1	0	0.2	0.2	0.5
$P(Y = n)$	0.4	0.1	0.2	0.1	0.2

 - (a) $P(1 \leq X \leq 3)$.
 - (b) $P(Y > 2)$.
 - (c) $E(X)$ and $E(Y)$.
 - (d) $E(X + 2Y)$.
 - (e) $\text{var}(X)$ and $\sigma(X)$.
 - (f) $\text{var}(Y)$ and $\sigma(Y)$.

11. An urn contains 10 pink and 10 green balls. 3 balls are drawn without replacement. If X is the discrete random variable counting the number of green balls selected, find
 - (a) The probability distribution for X .
 - (b) $P(X < 3)$.
 - (c) The expected value of X .
 - (d) The variance and standard deviation of X .
