

Lecture: Monday-Wednesday-Thursday, 4:35pm–5:40pm, Richards Hall 229.

Instructor: Evan Dummit, Lake Hall 571, edummit@northeastern.edu.

Instructor Office Hours: Monday-Thursday 11:45am–1:00pm + 3:00–4:00pm, or by appointment, in Lake Hall 571.

Problem Sessions: Wednesdays, time and location TBA.

Course Webpage: https://web.northeastern.edu/dummit/teaching_sp20_4751.html.

Course Textbook: The instructor will write lecture notes for the course (in lieu of an official textbook) as the semester progresses. The course will roughly follow the presentation from “Linear Algebra” (4th or 5th edition) by Friedberg, Insel, and Spence, but it is not necessary to purchase the textbook for this course.

Prerequisites: Math 1365 (Introduction to Mathematical Reasoning) or an equivalent familiarity with proof, and either Math 2331 (Linear Algebra) or Math 2341 (Differential Equations and Linear Algebra) or an equivalent familiarity with matrices.

Course Philosophy: Math 4571 is a second course in linear algebra that covers the material from a theoretical perspective. Linear algebra is a fundamental stepping stone to almost every area of advanced mathematics (including abstract algebra, functional analysis, algebraic topology, differential geometry, and applied and computational mathematics) and the sciences (especially scientific computation, theoretical physics, complex systems analysis, and applied engineering).

The primary theme of Math 4571 is to study vector spaces and linear transformations from a formal standpoint. Many applications of linear algebra can be treated entirely from a computational perspective, but this approach often leads to treating computations like a “black box”: the goal of Math 4571 is to gain a deep understanding of how these computations work, in addition to understanding their applications.

At the end of the course, you will have a solid grasp of the fundamentals of vector spaces, linear transformations, inner products, and quadratic forms, and how they can be used in a wide variety of applications. Success in this course thereby demands facility with the basic concepts, with the underlying theory, and with its applications.

Grades: Your course grade consists of **20% homework**, **40% midterms**, and **40% final exam**.

The homework score consists of the average of the written assignment scores, with the lowest score dropped.

There will be two 1-hour midterm exams (20% each) and a 2-hour final exam (40%).

An overall raw score of 92% will be **at least** an A, 89% will be **at least** an A-, 86% will be **at least** a B+, 82% will be **at least** a B, 79% will be **at least** a B-, 76% will be **at least** a C+, 72% will be **at least** a C, and 69% will be **at least** a C-.

If you feel that an assignment or exam has been misgraded, please talk to the instructor directly. Requests for regrading will not be considered more than two days past the date the assignment or exam was returned.

Exams: There will be two 1-hour midterm exams, along with a 2-hour final exam.

If you miss an examination for any reason, you will receive a 0; make-up exams will not be given except at the instructor's discretion.

The midterms are in class and scheduled for Wednesday, February 12th and Thursday, March 26th.

The final exam is scheduled TBA.

Homework Assignments: Written assignments will be assigned weekly and due by 6pm, typically on Thursdays.

Problem sessions will be held weekly on Wednesdays. The problem sessions provide you a place to work collaboratively on the homework assignments with help from the TA. **It is highly recommended to start the assignments early:** many problems will require substantial thought and effort to solve, even if the solution is ultimately fairly short. Do not fall into the trap of only starting the assignment the evening before it is due!

The lowest assignment grade is dropped, to provide you a cushion if an emergency arises and you cannot complete an assignment. For logistical reasons, extensions cannot be granted under any circumstances.

Written assignments should be organized carefully, neatly, and in complete sentences, with concise well-reasoned logical arguments. Cite any external resources used, and clearly label all problems. If you collaborated with any other students, write the names of all collaborators on the top of your assignment. If your assignment is more than one page long, use a staple or paperclip to affix the pages together. **Failure to adhere to any of these guidelines may result in point deductions, at the grader's discretion.**

Course Schedule: The course and lecture notes are tentatively organized into six chapters, as follows:

Weeks 1-2: Chapter 0 ~ Preliminaries: Vectors, matrices, determinants, fields, polynomials, induction

Weeks 2-3: Chapter 1 ~ Vector Spaces: Definition, subspaces, span, linear independence, bases and dimension

Weeks 4-6: Chapter 2 ~ Linear Transformations: Kernel and image, the nullity-rank theorem, algebraic properties, matrices associated to linear transformations, isomorphisms and inverses, change of basis and similarity

Week 6: Midterm 1, covers chapters 1-2.

Weeks 8-9: Chapter 3 ~ Inner Products: Inner products, norms, orthogonality, the Gram-Schmidt procedure, orthogonal complements, linear functionals, adjoint transformations, least-squares approximation, Fourier series

Weeks 10-12: Chapter 4 ~ Eigenvalues, Diagonalization, and the Jordan Canonical Form: Eigenvalues, eigenvectors, the characteristic polynomial, the Cayley-Hamilton theorem, diagonalization, Markov chains, generalized eigenvectors, the Jordan canonical form and its applications, Hermitian operators and the spectral theorem

Week 12: Midterm 2, covers chapters 3-4.

Weeks 13-14: Chapter 5 ~ Bilinear and Quadratic Forms: Bilinear forms, diagonalization, quadratic forms, the second derivatives test, Sylvester's law of inertia, applications of quadratic forms

Collaboration Policy: Mathematics is fundamentally a collaborative endeavor, and discussing the course material with others is an excellent way to solidify your own understanding. However, it is critical not to outsource your learning! You cannot expect to retain knowledge if you do not solve your homework problems yourself, whether because you relied on other people to explain to you how to do the problems, or because you relied too heavily on technological assistance.

On written assignments, you may work together with other people, **but you must write up your work independently**. If you use **any** external resources (e.g., wikipedia, stackexchange, other books beyond the course text or notes, other people, etc.) you must say **what results you are citing and where they are from**. If you happen to find a solution to an assigned problem online or elsewhere, it is academically dishonest to copy the solution and present it as your own work.

Please also note that 80% of your course grade is determined by the exams, on which collaboration is not allowed.

Attendance Policy: It is expected that you will attend every class. This course moves very fast, and it is quite possible to fall behind even if you only miss one day. If you miss class for any reason, it is highly advisable to consult the course lecture notes to catch up, and you may also wish to obtain notes from another student. It is your responsibility to be aware of all information announced in class, including modifications to the course syllabus or schedule, even if you are absent.

If you will be absent from a class activity due to a religious observance or practice, or for participation in a university-sanctioned event (e.g., university athletics), it is your responsibility to inform the instructor during the first week of class and provide appropriate documentation if required. Your instructor will work with you on alternative and reasonable arrangements for any time missed.

Statement on Academic Integrity: A commitment to the principles of academic integrity is essential to the mission of Northeastern University. Academic dishonesty violates the most fundamental values of an intellectual community and undermines the achievements of the entire University. Violations of academic integrity include (but are not limited to) cheating on assignments or exams, fabrication or misrepresentation of data or other work, plagiarism, unauthorized collaboration, and facilitation of others' dishonesty. Possible sanctions include (but are not limited to) warnings, grade penalties, course failure, suspension, and expulsion.

Statement on Accommodations: Any student with a disability is encouraged to meet with the instructor during the first week of classes to discuss accommodations. The student must bring a current Memorandum of Accommodations from the Office of Student Disability Services.

Statement on Classroom Behavior: Disruptive classroom behavior will not be tolerated.

In general, any behavior that impedes the ability of your fellow students to learn will be viewed as disruptive. Examples of disruptive behavior include, but are not limited to, ringing cell phones, listening to an audio player during class, constant talking, eating food noisily, or laptop usage (except for note-taking).

Statement on Inclusivity: Faculty are encouraged to address students by their preferred name and gender pronoun. If you would like to be addressed using a specific name or pronoun, please let your instructor know.

Statement on Evaluations: Students are requested to complete the TRACE evaluations at the end of the course.

Miscellaneous Disclaimer: The instructor reserves the right to change course policies, including the evaluation scheme of the course. Notice will be given in the event of any substantial changes.